

[14.6.103]

$$G(s) = \frac{Y(s)}{U(s)} = \frac{4}{s^2 + 5s + 4}$$

1) 1)

$$Y(s) = \frac{X_2(s)}{s}$$

$$sX_2(s) = 4U(s) - (5X_1(s) + 4Y(s))$$

$$s^2Y(s) = 4U(s) - 5sY(s) - 4Y(s)$$

$$(s^2 + 5s + 4)Y(s) = 4U(s)$$

$$\frac{Y(s)}{U(s)} = \frac{4}{s^2 + 5s + 4} //$$

2) 1)  $X_1 = Y$ 

$$X_1(s) = \frac{X_2(s)}{s} \rightarrow sX_1(s) = X_2(s)$$

$$sX_2(s) = 4U(s) - 5X_2(s) - 4X_1(s)$$

$$\begin{bmatrix} \dot{X}_1(t) \\ \dot{X}_2(t) \end{bmatrix} = \underbrace{\begin{bmatrix} 0 & 1 \\ -4 & -5 \end{bmatrix}}_{(A)} \begin{bmatrix} X_1(t) \\ X_2(t) \end{bmatrix} + \underbrace{\begin{bmatrix} 0 \\ 4 \end{bmatrix}}_{(b)} u(t)$$

1) 2-

$$sX_1(s) = -X_1(s) + U(s)$$

$$sX_2(s) = -4X_2(s) + U(s)$$

$$\rightarrow \dot{X}_1(t) = -X_1(t) + u(t)$$

$$\rightarrow \dot{X}_2(t) = -4X_2(t) + u(t)$$

$$\begin{bmatrix} \dot{X}_1(t) \\ \dot{X}_2(t) \end{bmatrix} = \underbrace{\begin{bmatrix} -1 & 0 \\ 0 & -4 \end{bmatrix}}_{(A)} \begin{bmatrix} X_1(t) \\ X_2(t) \end{bmatrix} + \underbrace{\begin{bmatrix} 1 \\ 1 \end{bmatrix}}_{(b)} u(t)$$

$$1) 2) X_1(s) = \frac{U(s)}{s+1}$$

$$X_2(s) = \frac{U(s)}{s+4}$$

$$Y(s) = \frac{4}{3} (X_1(s) - X_2(s))$$

$$Y(s) = \frac{4}{3} \left( \frac{U(s)}{s+1} - \frac{U(s)}{s+4} \right)$$

$$= \frac{4}{3} \frac{U(s)}{(s+1)(s+4)}$$

$$\frac{Y(s)}{U(s)} = \frac{4}{s^2 + 5s + 4} //$$

$$\dot{X}_1(t) = X_2(t)$$

$$\dot{X}_2(t) = -4X_2(t) + 4U(t)$$

$$\frac{d}{dt} f(t) \leftrightarrow sF(s) - f(0)$$

$$y = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} X_1(t) \\ X_2(t) \end{bmatrix}$$

$$(s+1)X_1(s) = U(s)$$

$$(s+4)X_2(s) = U(s)$$

$$y(t) = \frac{4}{3} X_1(t) - \frac{4}{3} X_2(t)$$

$$y(t) = \left[ \frac{4}{3} \quad -\frac{4}{3} \right] \begin{bmatrix} X_1(t) \\ X_2(t) \end{bmatrix} //$$

(c)